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# Antitrust Enforcement and Corporate Leniency Programs

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"Deterrence in Competition Policy"  
15th WZB Conference on Markets and Politics  
2nd Conference of the Research Network  
on Innovation and Competition Policy

October 17-18, 2008

# Introduction

## Challenges to Detering Collusion

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- 1 Challenge of ideas
- 2 Challenge of measurement
- 3 Challenge of implementation

# Introduction

## Challenges to Detering Collusion: Ideas

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- Challenge: Developing new policies.
- With an upper bound on penalties, it is critical to increase the probability that penalties are levied.
- Examples
  - Leniency programs
  - Whistleblowers
  - Screening

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## Challenges to Detering Collusion: Measurement

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- Challenge: Determining when a policy works.
- Policy objective is to impact the population of cartels, including
  - number of cartels
  - average duration of cartels
  - average overcharge
- Population of cartels is not observed, only the population of *discovered* cartels.

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## Challenges to Detering Collusion: Measurement

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- Number of discovered cartels may not be a good proxy for number of cartels.
- In response to a new policy, the number of discovered cartels could fall because
  - the policy is **effective** and there are fewer cartels
  - the policy is **ineffective** and thus fewer cartels are caught and convicted.
- The population of discovered cartels may not be a random sample of the population of cartels.
  - Unstable cartels may collapse before being caught  $\Rightarrow$  over-sampling more stable cartels.
  - Stable cartels may avoid detection  $\Rightarrow$  over-sampling less stable cartels.

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## Challenges to Detering Collusion: Implementation

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- Challenge: Having the competition authority properly implement a policy.
- Proper implementation includes
  - effective execution of the program itself (e.g., leniency program)
  - proper selection of complementary instruments (e.g., prosecution of non-lenieny cases)

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## Challenges to Detering Collusion: Implementation

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- Example: leniency program
- An abundance of leniency applications may cause the EC to reduce how many non-leniency cases it pursues.
- This could weaken the deterrence of relatively stable cartels.
- Would not an optimizing EC choose enforcement to minimize the cartel rate?
- *Why should the EC try to minimize the cartel rate?*

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## Objective of the Competition Authority

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- Taking a career concerns perspective,
  - the CA can only be rewarded based on *observable* measures of performance
  - the cartel rate is not observable
  - therefore, the CA will not be concerned with the cartel rate
- Will the CA undervalue deterrence?
- Vitamins: US DOJ and Hoffman La Roche.
  - Guidelines: Fine between \$1.3B and \$2.6B.
  - Actual fine: \$0.5B.
- Proper design of a policy should take into account the incentives of the CA.



# Introduction

## Overview of Research

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- Competition authority faces a resource constraint
  - Firms use the leniency program if they think it is sufficiently likely they'll be penalized.
  - Likelihood of being penalized depends on the CA's caseload which includes both leniency and non-lenieny cases.
- Competition authority influences its caseload.
- Main findings
  - Holding the CA's enforcement policy fixed, a leniency program lowers the cartel rate.
  - Allowing the CA to adjust its enforcement policy, a leniency program can either raise or lower the cartel rate.

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## Firm Environment

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- In each market,  $n$  firms interact in a Prisoners' Dilemma - *collude* or *compete*.
  - All collude: each firm earns  $\pi > 0$ .
  - All compete: each firm earns  $\alpha\pi$ ,  $\alpha \in [0, 1)$ .
  - A firm competes and all others collude: deviator earns  $\eta\pi$ ,  $\eta > 1$ .
- Stochastic market conditions
  - $\pi$  is iid with cdf  $H : [\underline{\pi}, \bar{\pi}] \rightarrow [0, 1]$ .
  - $\mu \equiv \int \pi H'(\pi) d\pi$ .
  - $\pi$  is observed prior to firms deciding between *collude* and *compete*

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## Firm Environment

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- State of an industry: *cartel* or *non-cartel*.
- If firms are not cartelized then each firm earns  $\alpha\pi$ .
- If firms are cartelized then each firm decides
  - to *collude* or *compete* and
  - whether to apply for leniency.
- Penalization - leniency program is not used.
  - Cartel is discovered, prosecuted, and convicted with probability  $\sigma \in [0, 1]$ .
  - If convicted, each firm pays a (per period) penalty of  $F$ .
- Penalization - leniency program is used.
  - First firm "in the door" receives a penalty of  $\theta F$ ,  $\theta \in [0, 1]$ .
  - All other firms pay  $F$ .

# Model

## Evolution of Cartel Status

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- If an industry enters the period as a cartel then it exits the period as a cartel iff
  - all firms chose *collude*
  - no firm applied for leniency
  - the CA did not discover, prosecute, and convict.
- If an industry enters the period not as a cartel then
  - with probability  $\kappa$  it becomes a cartel
  - with probability  $1 - \kappa$  it remains a competitive industry
- Industry heterogeneity
  - Industry type:  $\eta$  controls the propensity to cheat.
  - Distribution of industries, cdf  $G : [\underline{\eta}, \bar{\eta}] \rightarrow [0, 1]$ .

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## Sequence of Events

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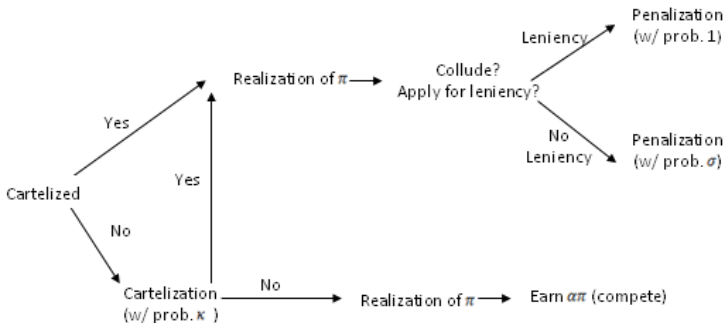
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# Model

## Antitrust Enforcement Technology

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- $\sigma = q \times r \times s$  is the probability that a cartel pays penalties (when no firm used the leniency program).
  - $q$  is the probability the cartel is discovered
  - $r$  is the probability the CA prosecutes a discovered cartel
  - $s$  is the probability that the CA is successful in a prosecution
- Probability of a conviction:

$$s = p(\lambda L + R) = \frac{\tau}{\xi + v(\lambda L + R)^\rho}$$

- $L$  is the number (or mass) of leniency cases
- $R$  is the number of non-lenieny cases
- $\lambda \in [0, 1]$ ,  $v > 0$ ,  $\rho \geq 1$ ,  $\tau \in (0, 1]$ ,  $\xi \geq \tau$

# Equilibrium

## Collusion

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- $Y$  is firm value when firms are in the cartel state.
- $W$  is firm value when firms are not in the cartel state.
- Incentive compatibility constraint:

$$(1 - \delta) \pi + \delta [(1 - \sigma) Y + \sigma (W - F)] \geq (1 - \delta) \eta \pi + \delta [W - \min \{\sigma F, \theta F\}]$$

- Endogenizing penalty:  $F = \gamma (Y - \alpha \mu)$ ,  $\gamma > 0$ .

$$\pi \leq \frac{(Y - W) - \delta [\sigma - \min \{\sigma, \theta\}] \gamma (Y - \alpha \mu)}{(1 - \delta) (\eta - 1)}$$

$$\pi \leq \phi(Y, W, \eta)$$

# Equilibrium

## Collusion

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- $(Y, W)$  are equilibrium values iff:

$$W = (1 - \kappa) [(1 - \delta) \alpha \mu + \delta W] + \kappa Y \quad (1)$$

$$Y = \int_{\underline{\pi}}^{\phi(Y, \sigma, \eta)} \{ (1 - \delta) \pi + \delta [(1 - \sigma) Y + \sigma (W - F)] \} \times H'(\pi) d\pi \quad (2)$$
$$+ \int_{\phi(Y, \sigma, \eta)}^{\bar{\pi}} [(1 - \delta) \alpha \pi + \delta W - \delta \beta(\sigma, \theta) F] H'(\pi) d\pi$$

- $Y^*$  is the maximal solution:

$$Y^*(\sigma, \eta) \equiv \max \{ Y \in [\alpha \mu, \mu] : (Y, W) \text{ solve (1)-(2)} \}.$$



# Equilibrium

## Markov Process on Cartel Birth and Death

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- Incentive compatibility constraint:

$$\pi \leq \phi(Y^*(\sigma, \eta), W^*(\sigma, \eta), \eta) \equiv \phi^*(\sigma, \eta)$$

- $C(\sigma, \eta)$  is the proportion of cartels among type- $\eta$  industries.
- Stationary proportion of type- $\eta$  industries which are not cartelized:

$$1 - C(\sigma, \eta) = [1 - C(\sigma, \eta)] \times \\ [(1 - \kappa) + \kappa(1 - H(\phi^*)) + \kappa H(\phi^*) \sigma] \\ + C(\sigma, \eta) [(1 - H(\phi^*)) + H(\phi^*) \sigma]$$

- $\kappa$  is the probability a competitive industry cartelizes.
- $H(\phi^*)$  is the probability that a cartel internally collapses.
- $\sigma$  is the probability that a cartel collapses because it is convicted.

# Equilibrium

## Stationary Distribution on Cartels

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- Solve for  $C(\sigma, \eta)$  :

$$C(\sigma, \eta) = \frac{\kappa H(\phi^*(\sigma, \eta))}{1 - (1 - \sigma - \kappa) H(\phi^*(\sigma, \eta))}$$

- Rate of cartelized industries:

$$\begin{aligned} C(\sigma) &= \int_{\underline{\eta}}^{\bar{\eta}} C(\sigma, \eta) G'(\eta) d\eta \\ &= \int_{\underline{\eta}}^{\bar{\eta}} \left[ \frac{\kappa H(\phi^*(\sigma, \eta))}{1 - (1 - \sigma - \kappa) H(\phi^*(\sigma, \eta))} \right] G'(\eta) d\eta \end{aligned}$$

# Equilibrium

## Probability of Conviction

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- $\sigma = q \times r \times s$  is the probability that a cartel is discovered ( $q$ ), prosecuted ( $r$ ), and convicted ( $s$ ).
- Leniency cases:

$$L(qrs) = \int_{\underline{\eta}}^{\bar{\eta}} [1 - H(\phi^*(qrs, \eta))] C(qrs, \eta) G'(\eta) d\eta.$$

- Non-leniency cases:

$$R(qrs) = qrC(qrs).$$

# Equilibrium

## Conviction and Enforcement Rate

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- Equilibrium conviction rate,  $s^*(r)$ :

$$s^* = p(\lambda L(qrs^*) + R(qrs^*)).$$

- Optimal enforcement (or prosecution) rate:

$$r^* = \arg \max L(qrs^*(r)) + qrs^*(r) C(qrs^*(r)).$$

# Numerical Analysis

## Parameterization

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- Leniency policy
  - A firm with leniency pays  $\theta F$ .
  - A firm without leniency pays  $F$ .
- Policy comparison
  - No leniency:  $\theta = 1$ .
  - Full leniency:  $\theta = 0$ .
- Parameters
  - Probability a cartel is discovered:  $q = .2$
  - Probability a competitive industry cartelizes:  $\kappa = .05$
  - Market conditions:  $H(\pi) : [1, \infty) \rightarrow [0, 1]$  is a log-normal distribution.
  - Industry types:  $G(\eta) : [1.1, \infty) \rightarrow [0, 1]$  is a log-normal distribution.

# Numerical Analysis

## Method

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- 1 Given  $\sigma (= q \times r \times s)$ , solve for equilibrium collusive behavior,  $\phi^*(\sigma, \eta)$ , for each industry type  $\eta$ . Collude iff  $\pi \leq \phi^*(\sigma, \eta)$ .
- 2 Given  $\phi^*(\sigma, \eta)$ , define the Markov process on cartel birth and death. Solve for the stationary distribution on cartels for each industry type  $\eta$  and aggregate over types to derive the stationary cartel rate,  $C(\sigma)$ .
- 3 Given  $C(\sigma)$ , solve for the equilibrium conviction rate,  $s^*$ :

$$s^* = p(\lambda L(qrs^*) + R(qrs^*))$$

- 4 Given  $s^*(r)$ , solve for the value for  $r$  which maximizes the antitrust authority's objective:

$$r^* = \arg \max L(qrs^*(r)) + qrs^*(r) C(qrs^*(r))$$

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Table 1: Case of No Leniency Program ( $\theta = 1$ )

$r$	prob. of conviction	prob. of penalties	cartel rate	cartel duration
0%	.801	.000	.326	155.57
10%	.691	.014	.230	42.54
20%	.613	.025	.180	26.92
30%	.562	.034	.149	20.49
40%	.530	.042	.127	16.78
50%	.512	.051	.108	14.17
60%	.508	.061	.091	12.10
70%	.520	.073	.075	10.27
80%	.547	.088	.059	8.68
90%	.578	.104	.047	7.37
100%	.615	.123	.036	6.28

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Table 2: Case of Full Leniency Program ( $\theta = 0$ )

$r$	prob. of conviction	prob. of penalties*	cartel rate	cartel duration
0%	.801	.000	.326	155.57
10%	.707	.024	.163	46.27
20%	.674	.040	.113	26.97
30%	.666	.056	.081	18.82
40%	.682	.074	.056	14.01
50%	.711	.095	.036	10.82
60%	.748	.119	.020	8.59
70%	.775	.145	.011	7.01
80%	.789	.174	.005	5.82
90%	.799	.204	.001	4.92
100%	.801	.277	.0001	3.62

\*Includes both leniency and non-lenieny cases.

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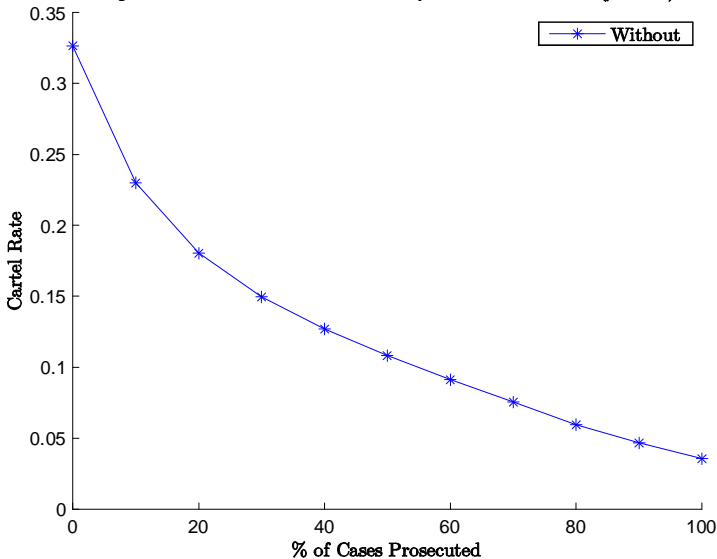
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Figure 1: Effects of Prosecution Policy on the Cartel Rate ( $\rho = 1.5$ )



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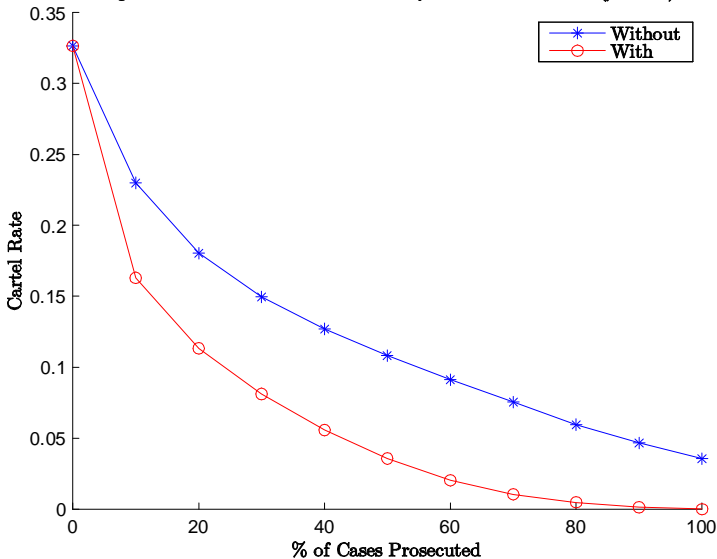
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Figure 1: Effects of Prosecution Policy on the Cartel Rate ( $\rho = 1.5$ )



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**Property 1** *Given the competition authority's enforcement policy (i.e.,  $r$  is fixed), the introduction of a leniency program reduces the cartel rate.*

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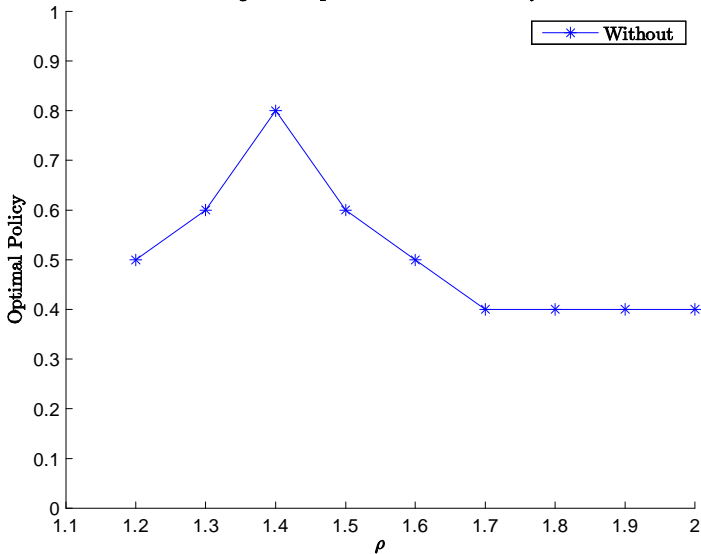
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Figure 2: Optimal Prosecution Policy



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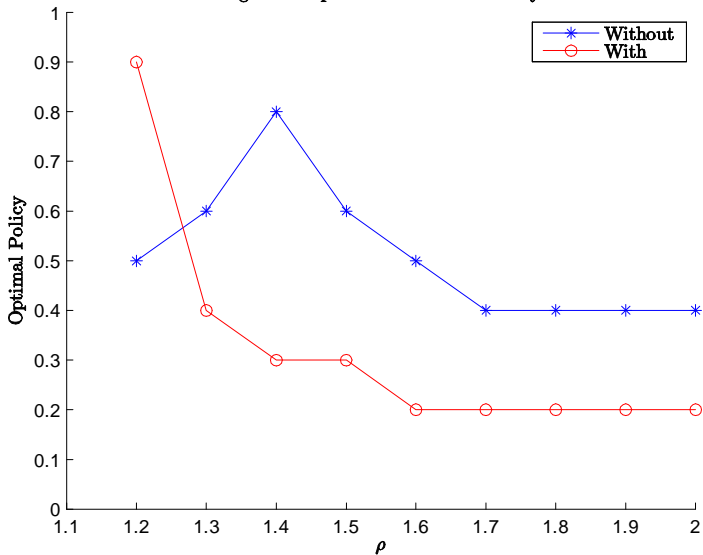
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Figure 2: Optimal Prosecution Policy



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**Property 1** Given the competition authority's enforcement policy (i.e.,  $r$  is fixed), the introduction of a leniency program reduces the cartel rate.

**Property 2** *Generally, the introduction of a leniency program results in the competition authority pursuing a less aggressive enforcement policy (i.e., it prosecutes a smaller fraction of non-lenieny cases).*

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Table 3: Effect of a Leniency Program on the Cartel Rate

$\rho$	$r_{NL}^*$	cartel rate ( $r = r_{NL}^*$ )		$r_L^*$	cartel rate ( $r = r_L^*$ )
		no leniency	leniency		
1.2	50%	.240	.141	90%	.133
1.3	60%	.203	.065	40%	.101
1.4	80%	.139	.005	30%	.094
1.5	60%	.091	.020	30%	.081
1.6	50%	.087	.032	20%	.107
1.7	40%	.099	.047	20%	.105
1.8	40%	.093	.044	20%	.101
1.9	40%	.091	.044	20%	.101
2.0	40%	.089	.044	20%	.100

NL = no leniency program, L = leniency program

# Preliminary Results

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- Property 1** Given the competition authority's enforcement policy (i.e.,  $r$  is fixed), the introduction of a leniency program reduces the cartel rate.
- Property 2** Generally, the introduction of a leniency program results in the competition authority pursuing a less aggressive enforcement policy (i.e., it prosecutes a smaller fraction of non-lenieny cases).
- Property 3** *When the competition authority chooses its optimal enforcement policy, the introduction of a leniency program can either lower or raise the cartel rate (depending on the parameter values).*



# Future Directions

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- With a leniency program, should a competition authority's budget be increased or decreased?
- What is the impact of a leniency program that accepts applications after an investigation has started?
- What are alternative objectives for a competition authority?
- What is the optimal incentive scheme for a competition authority?